

Digital Logic Design HW Answer
【Unit 3 & Unit 4】

3.8

$$A' + BD' + B'D$$

3.10

(a) $WYZ' + WY'Z + XW'$

(c) $(A' + C' + D')(B + C' + D)(A + C + D)$

3.17

(f)

$$\begin{aligned}(x \equiv y) \equiv z &= (xy + x'y') \equiv z = (xy + x'y')z + (xy' + x'y)z' \\&= xyz + x'y'z + xy'z' + x'yz' = x(yz + y'z') + x'(y'z + yz') \\&= x(yz + y'z') + x'(yz + yz')' \\&= x \equiv (yz + y'z') \\&= x \equiv (y \equiv z)\end{aligned}$$

(g)

$$\begin{aligned}(x \equiv y)' &= (xy + x'y')' = (x' + y')(x + y) = x'y + xy' \\&= x' \equiv y = xy' + x'y = x \equiv y'\end{aligned}$$

3.18

(f)

$$\begin{aligned}(x \oplus y) \oplus z &= (xy' + x'y) \oplus z = (xy' + x'y)z' + (xy' + x'y)'z \\&= xy'z' + x'yz' + xyz + x'y'z = x(yz + y'z') + x'(yz' + y'z) \\&= x(yz' + yz)' + x'(yz' + y'z) = x \oplus (yz + y'z') = x \oplus (y \oplus z)\end{aligned}$$

(g)

$$\begin{aligned}(x \oplus y)' &= (xy' + x'y)' = (x' + y)(x + y') = x'y' + xy \\&= x' \oplus y = xy + x'y' = x \oplus y'\end{aligned}$$

3.20

(a)

$$xy \oplus xz = xy(x' + z') + (x' + y')xz = xyz' + x'y'z = x(yz' + y'z) = x(y \oplus z)$$

(b)

For $y = 1$, the left hand side is $x + z'$ but the right hand side is $x'z'$ which are not equal.

(c)

For $y = 0$, the left hand side is xz' but the right hand side is $x' + z'$ which are not equal.

(d)

$$\begin{aligned}(x + y) &\equiv (x + z) = (x + y)(x + z) + (x + y)'(x + z)' = x + yz + (x'y')(x'z') \\ &= x + yz + x'y'z' = x + yz + y'z' = x + (y \equiv z)\end{aligned}$$

3.25

(f)

$$A'BD + B'EF + CDE'G$$

(g)

$$abd + b'd' + c'd$$

3.31

(a)

VALID:

$$\text{LHS} = (X' + Y')(X \oplus Z) + (X + Y)(X \oplus Z)$$

$$\begin{aligned}&= (X' + Y')(X'Z' + XZ) + (X + Y)(X'Z + XZ') \\ &= X'Z' + X'YZ' + XY'Z + X'YZ + XZ' + XYZ' \\ &= X'Z' + (XY' + X'Y)Z + XZ' \\ &= Z' + Z(X \oplus Y) = Z' + (X \oplus Y) = \text{RHS}\end{aligned}$$

(b)

VALID:

$$\text{LHS} = (W' + X + Y')(W + X' + Y)(W + Y' + Z)$$

$$\begin{aligned}&= (W' + X + Y')(W + (X' + Y)(Y' + Z)) \\ &= (W' + X + Y')(W + (X'Y' + YZ + X'Z)) \\ &= W'X'Y' + W'X'Z + W'YZ + WX + WY' + XYZ + Y'W + X'Y' + X'Y'Z \\ &= W'YZ + XYZ + WX + X'Y' = \text{RHS}\end{aligned}$$

(c)

VALID:

$$\begin{aligned}\text{RHS} &= (A' + C)(A + D')(B + C' + D) \\ &= (A'D' + AC + CD')(B + C' + D)\end{aligned}$$

$$\begin{aligned}&= A'BD' + A'C'D' + ABC + ACD + BCD \\ &= ABC + A'C'D' + A'BD' + ACD = \text{LHS}\end{aligned}$$

3.38

(a)

$x(y + a') = x(y + b')$ implies that
 $0 = x(y + a') \oplus x(y + b')$

$$\begin{aligned} &= x(y + a')(x' + y'b) + (x' + y'a)x(y + b') \\ &= xy'b(y + a') + xy'a(y + b') \\ &= xy'a'b + xy'ab' = xy'(a'b + ab') \\ &= xy'(a \oplus b) \end{aligned}$$

which implies that $x=1$ or $y=0$ or $a=b$.

(b)

$a'b + ab' = a'c + ac'$ implies that
 $0 = (a'b + ab') \oplus (a'c + ac')$

$$\begin{aligned} &= (a'b + ab')(ac + a'c') + (ab + a'b')(a'c + ac') \\ &= a'bc' + ab'c + abc' + a'b'c \\ &= a'(bc' + b'c) + a(bc' + b'c) = bc' + b'c = b \oplus c \end{aligned}$$

which implies that $b = c$.

4.3

$$F_1 = \sum m(0, 4, 5, 6); F_2 = \sum m(0, 3, 4, 6, 7); F_1 + F_2 = \sum m(0, 3, 4, 5, 6, 7)$$

General rule: $F_1 + F_2$ is the sum of all minterms that are present in either F_1 or F_2 .

$$\begin{aligned} \text{Proof: Let } F_1 &= \sum_{i=0}^{2^n-1} a_i m_i; F_2 = \sum_{j=0}^{2^n-1} b_j m_j; F_1 + F_2 = \sum_{i=0}^{2^n-1} a_i m_i + \sum_{j=0}^{2^n-1} b_j m_j = a_0 m_0 + a_1 m_1 + a_2 m_2 + \dots \\ &+ b_0 m_0 + b_1 m_1 + b_2 m_2 + \dots = (a_0 + b_0) m_0 + (a_1 + b_1) m_1 + (a_2 + b_2) m_2 + \dots = \sum_{i=0}^{2^n-1} (a_i + b_i) m_i \end{aligned}$$

4.4

(a) 16

(b)

$x \ y$	z_0	z_1	z_2	z_3	z_4	z_5	z_6	z_7	z_8	z_9	z_{10}	z_{11}	z_{12}	z_{13}	z_{14}	z_{15}
0 0	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1
0 1	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
1 0	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
1 1	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
	0	$x'y'$	$x'y$	$x'y'$	$x'y$	y'	$x'y'+xy'$	$x'+y'$	xy	$x'y'+xy$	y	$x'+y$	x	$x+y'$	$x+y$	1

4.6

(a) set don't care $d_1 = 1$ and $d_5 = 0$, $F = A'B' + AB$

(b) set all don't care to 0, $G = C$

4.9

(a)

$$\sum m(0, 1, 4, 5, 6)$$

(b)

$$\prod M(2, 3, 7)$$

(c)

$$\sum m(2, 3, 7)$$

(d)

$$\prod M(0, 1, 4, 5, 6)$$

4.25

(a)

$$\sum m(5, 6, 7, 10, 11, 13, 14, 15) = \prod M(0, 1, 2, 3, 4, 8, 9, 12)$$

(b)

$$\sum m(0, 2, 4, 6) = \prod M(1, 3, 5, 7, 8, 9, 10, 11, 12, 13, 14, 15)$$

(c)

$$\sum m(7, 11, 13, 14, 15) = \prod M(0, 1, 2, 3, 4, 5, 6, 8, 9, 10, 12)$$

(d)

$$\sum m(4, 8, 12, 13, 14) = \prod M(0, 1, 2, 3, 5, 6, 7, 9, 10, 11, 15)$$

4.45

(a)

E_1	E_0	s_i	c_{i+1}
0	0	$s_i = a_i \oplus b_i \oplus c_i$	$c_{i+1} = a_i b_i + a_i c_i + b_i c_i$
0	1	$s_i = a_i \oplus b_i \oplus c_i$	$c_{i+1} = a_i' b_i + a_i' c_i + b_i c_i$
1	0	$s_i = a_i \oplus b_i$	$c_{i+1} = a_i b_i + a_i c_i + b_i c_i$
1	1	$s_i = a_i \oplus b_i \oplus a_i b_i$	$c_{i+1} = a_i' b_i + a_i' c_i + b_i c_i$

(b)

E_1	E_0	Function
0	0	Add (A , B)
0	1	Subt (A , B)
1	0	XOR (A , B)
1	1	OR (A , B)

(hint: ignore the carry out's function in $E_1=1, E_0=0$ and $E_1=1, E_0=1$)